

On the buoyancy-driven theory of the Atlantic Meridional Overturning Circulation

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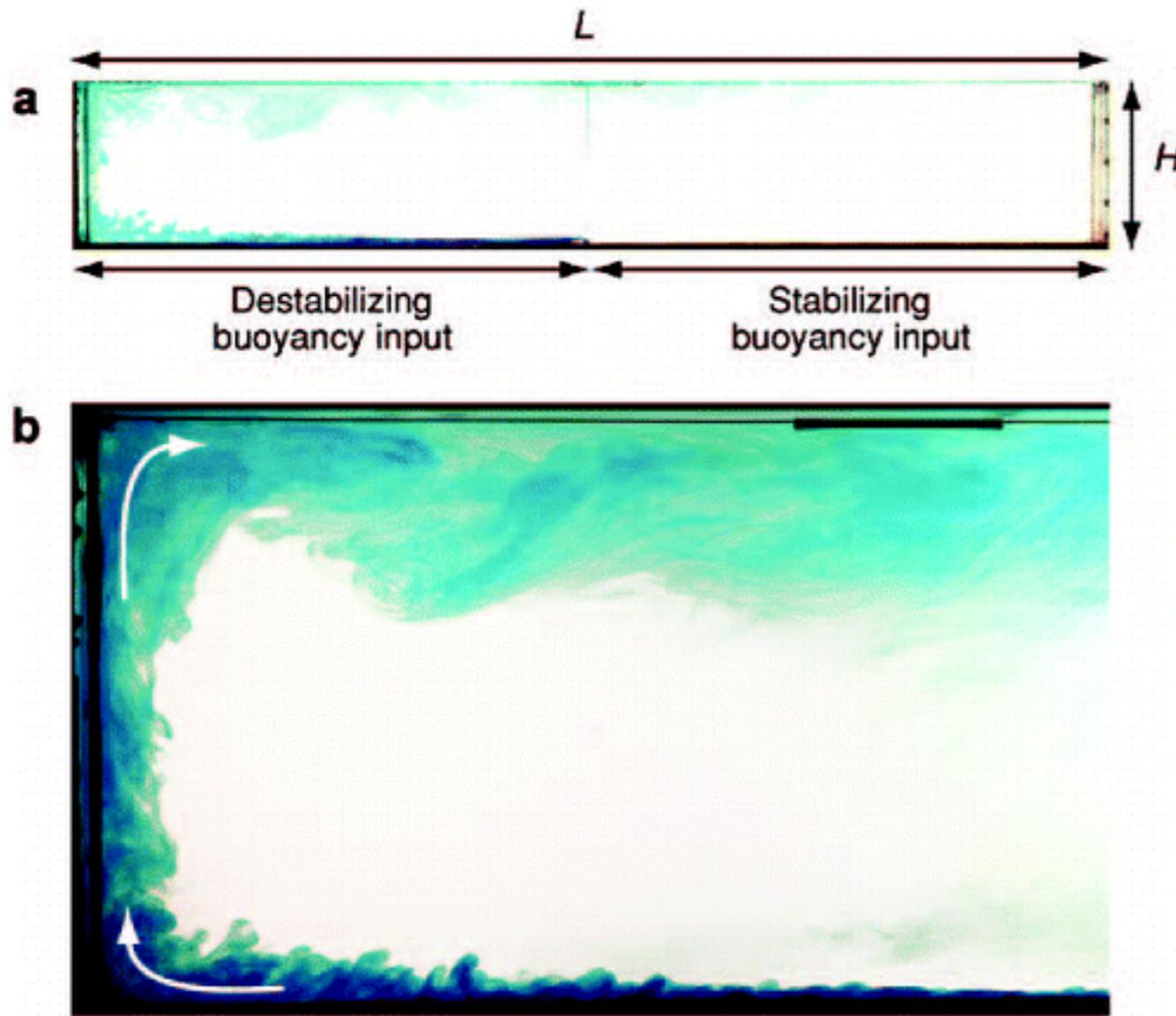
AMOC Meeting, Brest, 4 May 2017

Outline

- A survey of thermodynamic and mechanical effects on AMOC strength
- Buoyancy-Driven theory of AMOC and Theory of Available Potential Energy
- Importance of ocean state for estimating driving forces
- Conclusions

**Strength of AMOC is determined
both by thermodynamic and
mechanical effects**

AMOC strength increases with strength of buoyancy source

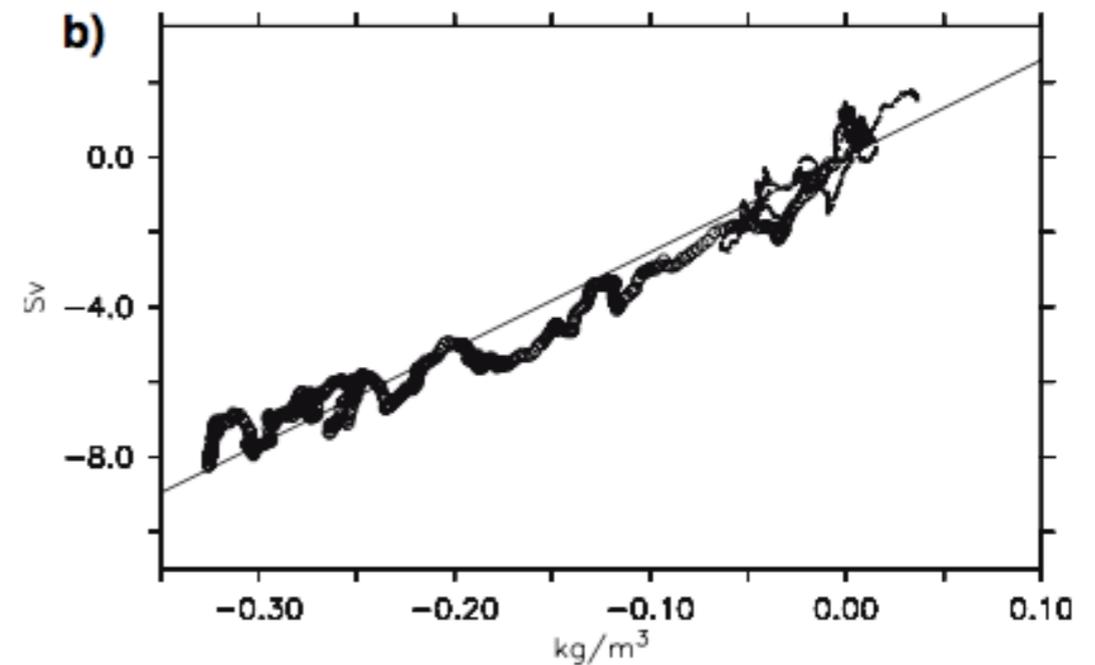
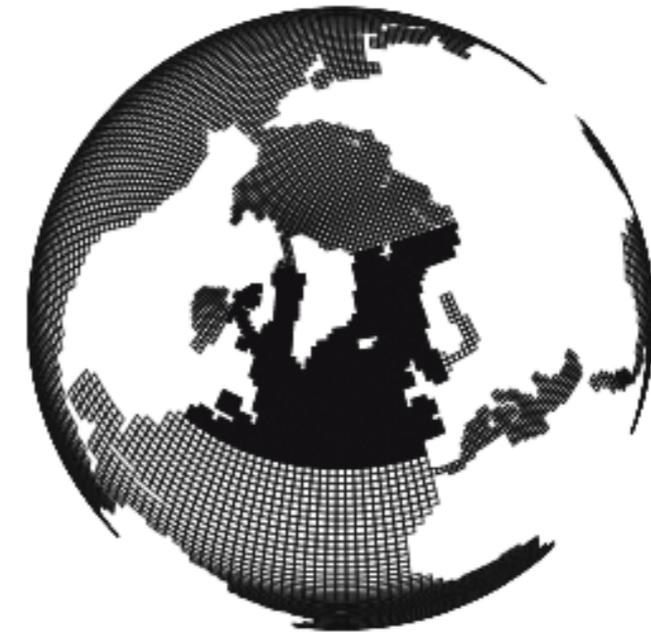


AR Hughes GO, Griffiths RW. 2008.
Annu. Rev. Fluid Mech. 40:185–208

Laboratory Experiments

GCM world:
Swingedouw et al. (2007)

a) Convection sites region



Bryan (JPO, 1987): Thermocline depth and AMOC strength increase with vertical diffusivity

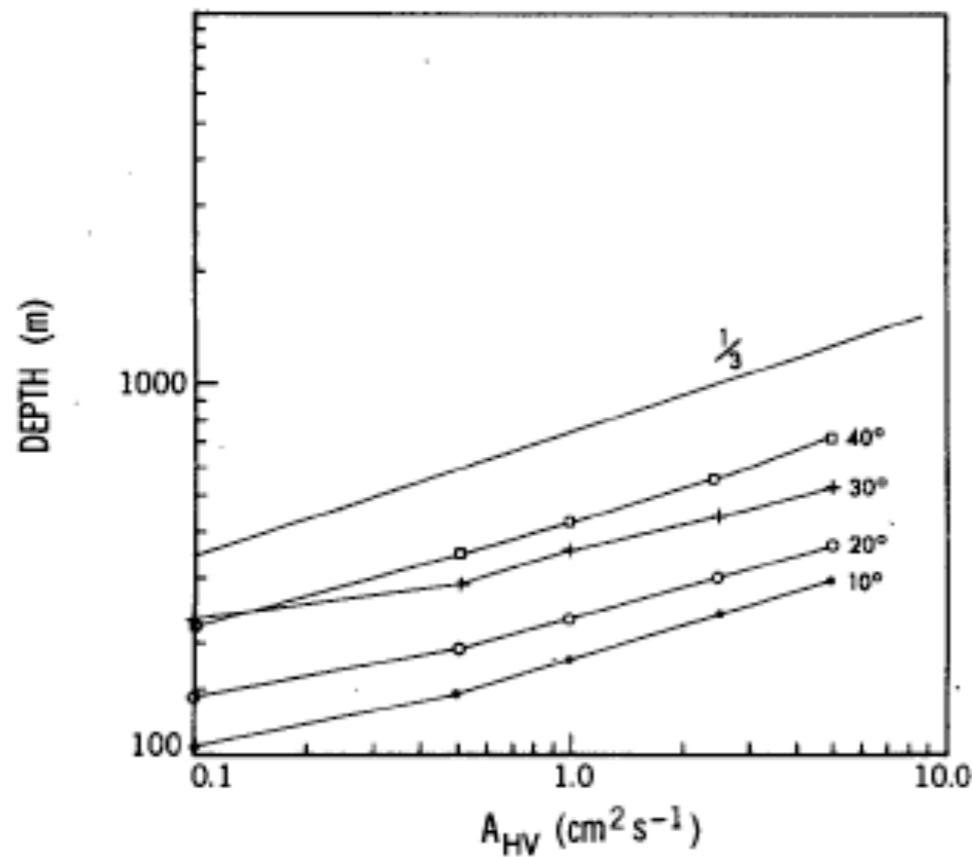


FIG. 4. Dependence of thermocline e-folding scale depth on vertical diffusivity at selected latitudes.

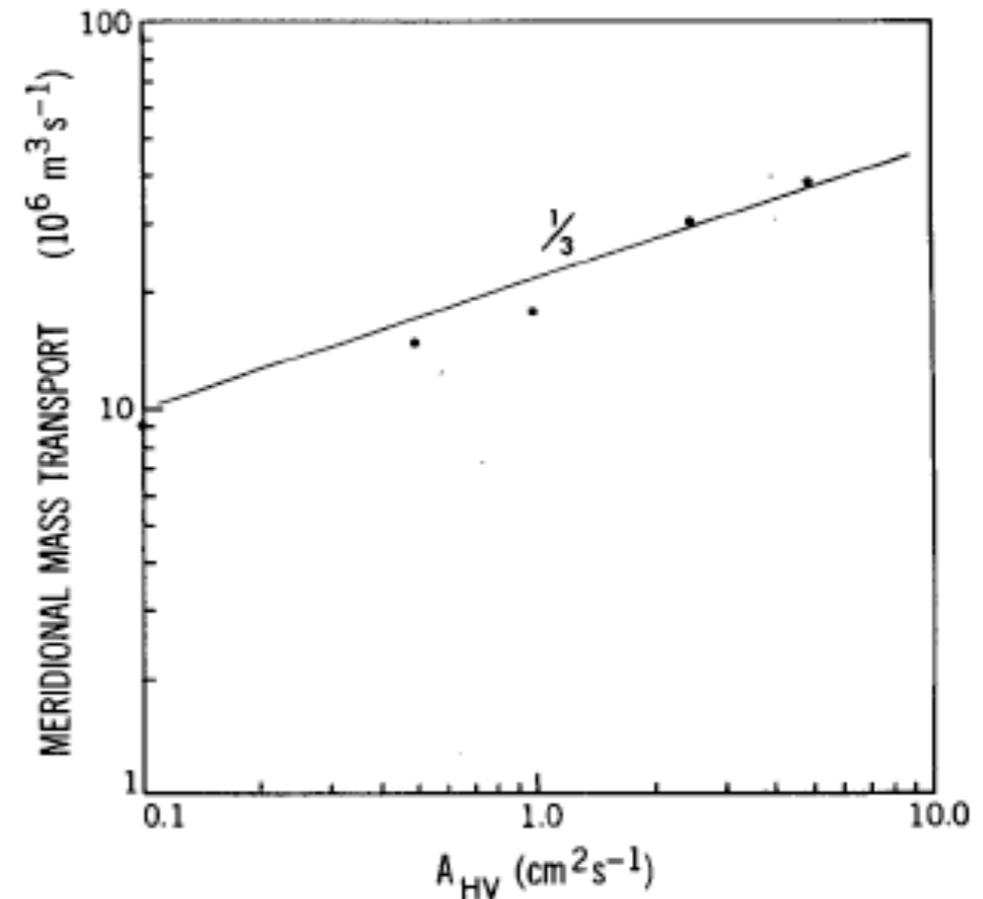


FIG. 8. Dependence of meridional overturning streamfunction on vertical diffusivity.

Vertical mixing is primarily driven by winds and tides, hence mechanically-driven

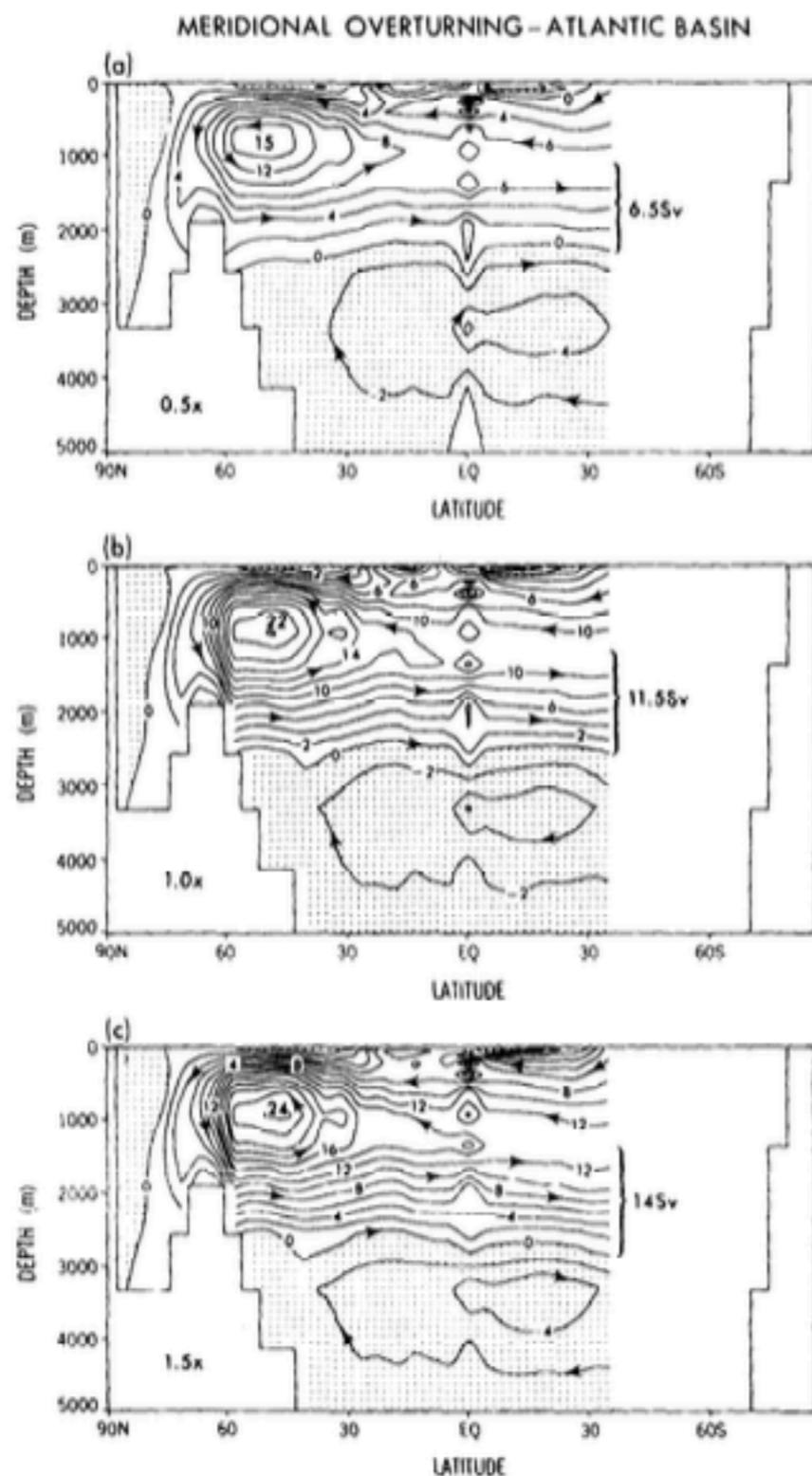
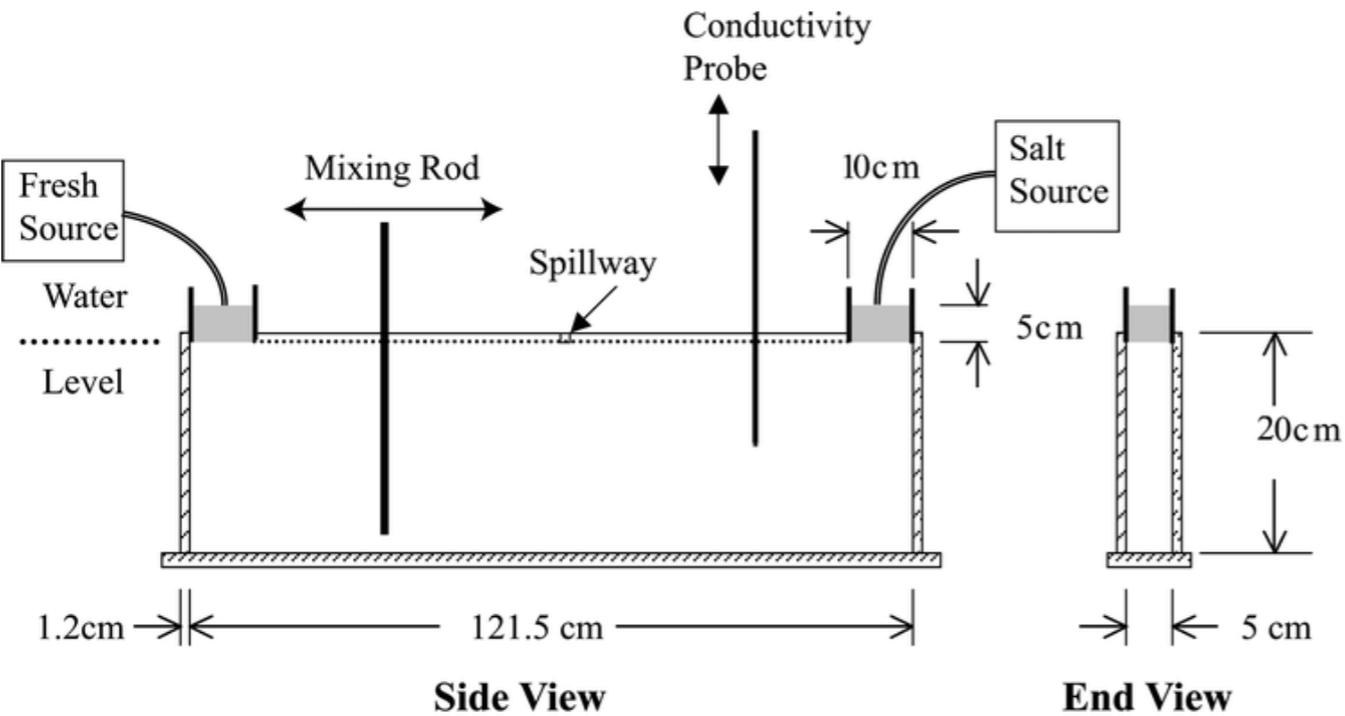


Fig. 3. Meridional overturning in the Atlantic basin from the 0.5 \times (top), 1.0 \times (middle) and 1.5 \times (bottom) wind sensitivity experiments. The flow between stream lines is 2 Sv. The outflow of deep water (of North Atlantic origin) through the South Atlantic scales with the wind stress applied south of 30°S. The model's outflow is indicated by the bracketed streamlines between roughly 1300 and 2600 m.

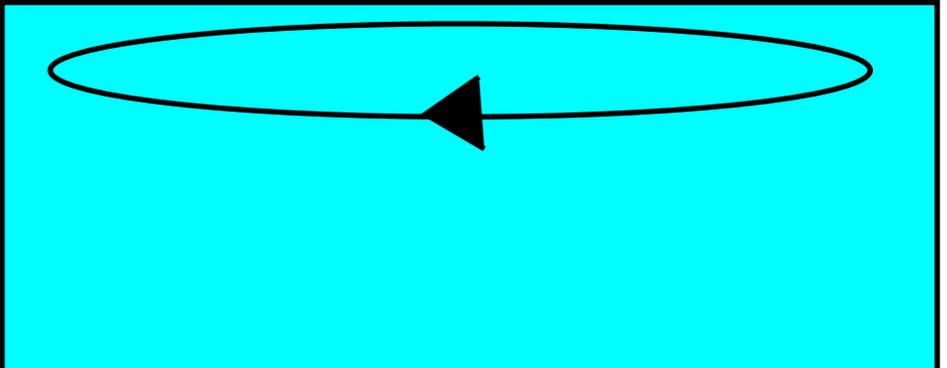
Drake Passage Effect Toggweiler and Samuels (1993)

**Strength of AMOC
appears to linearly
increase with
strength of zonal
wind at altitude of
Drake Passage**

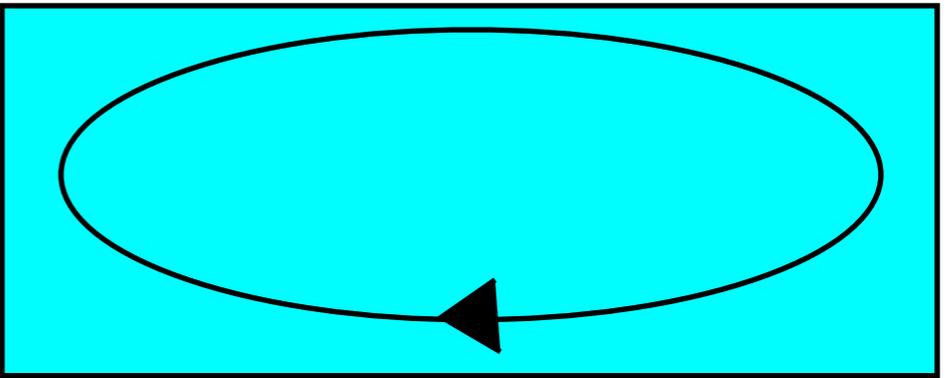
Whitehead and Wang (JPO,2008)



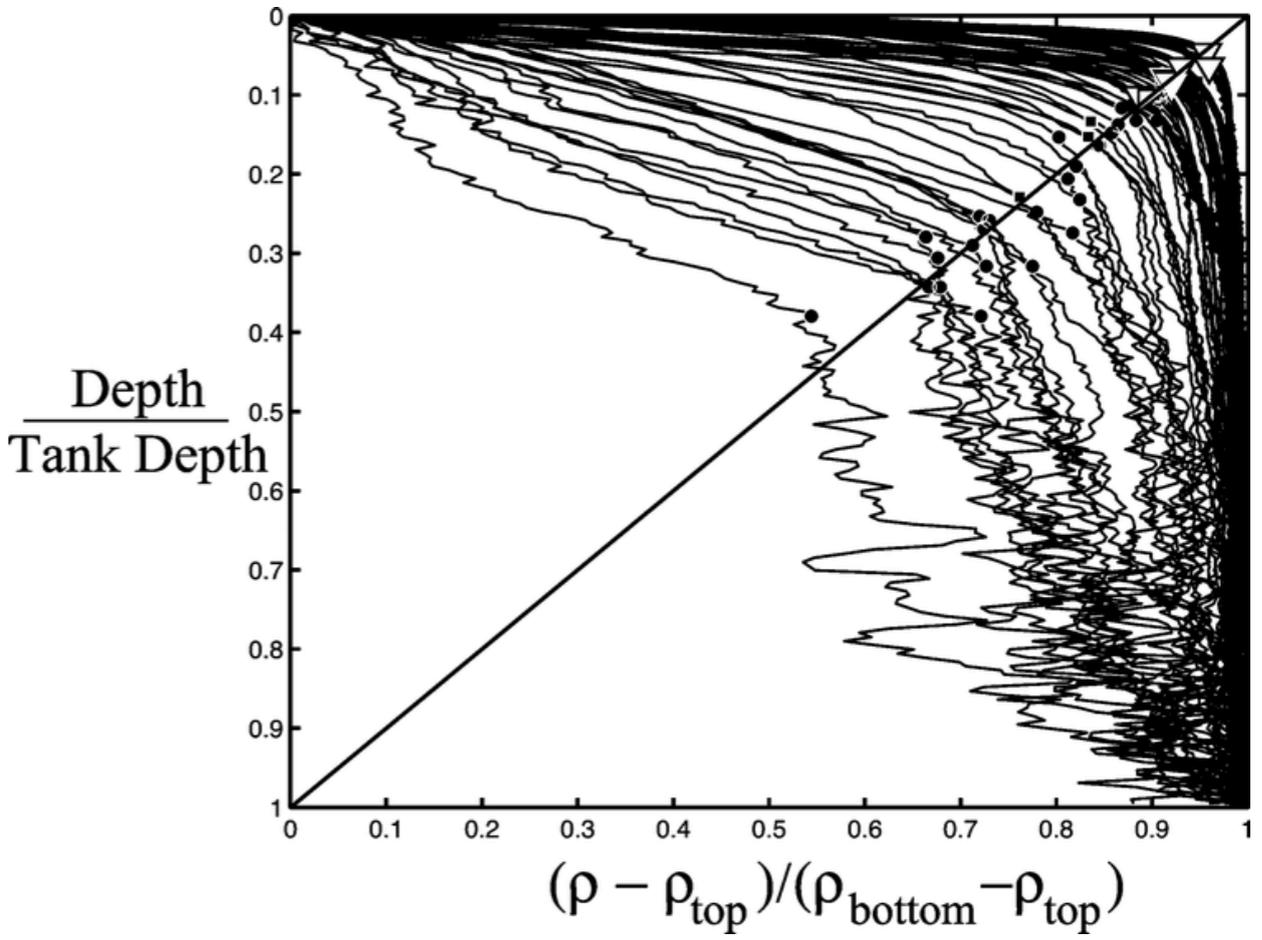
Buoyancy only



Buoyancy + Stirring



Turbulent stirring causes overturning to increase



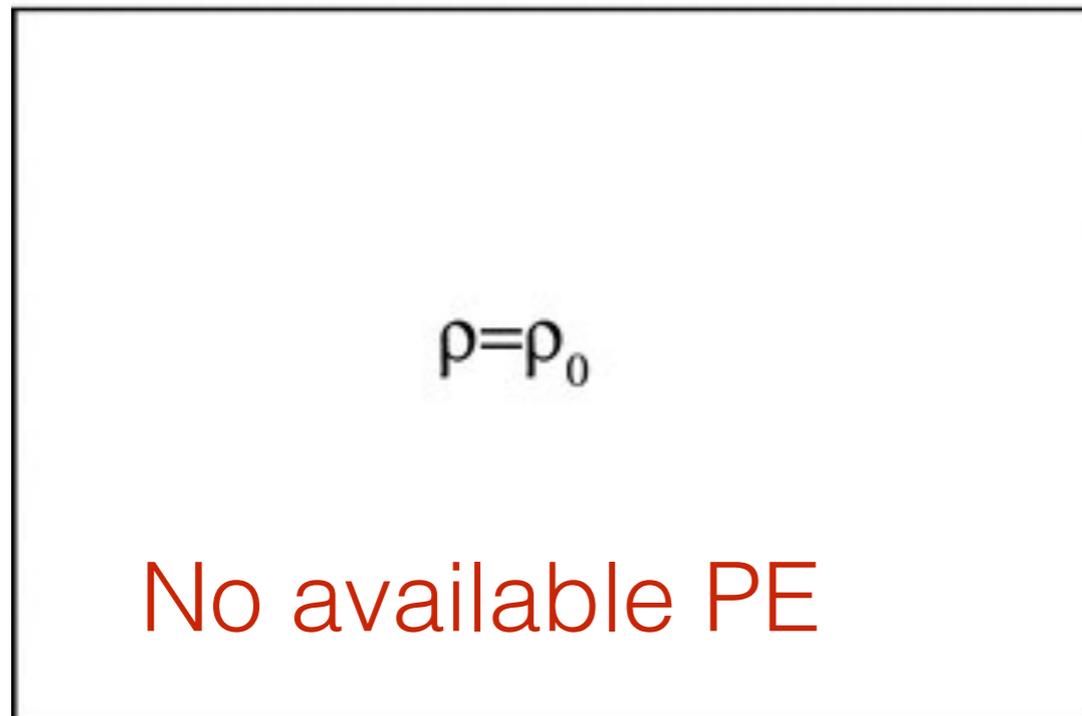
Buoyancy-Driven or Mechanically-Driven?

What about
Mechanically-controlled buoyancy-driven
circulation?

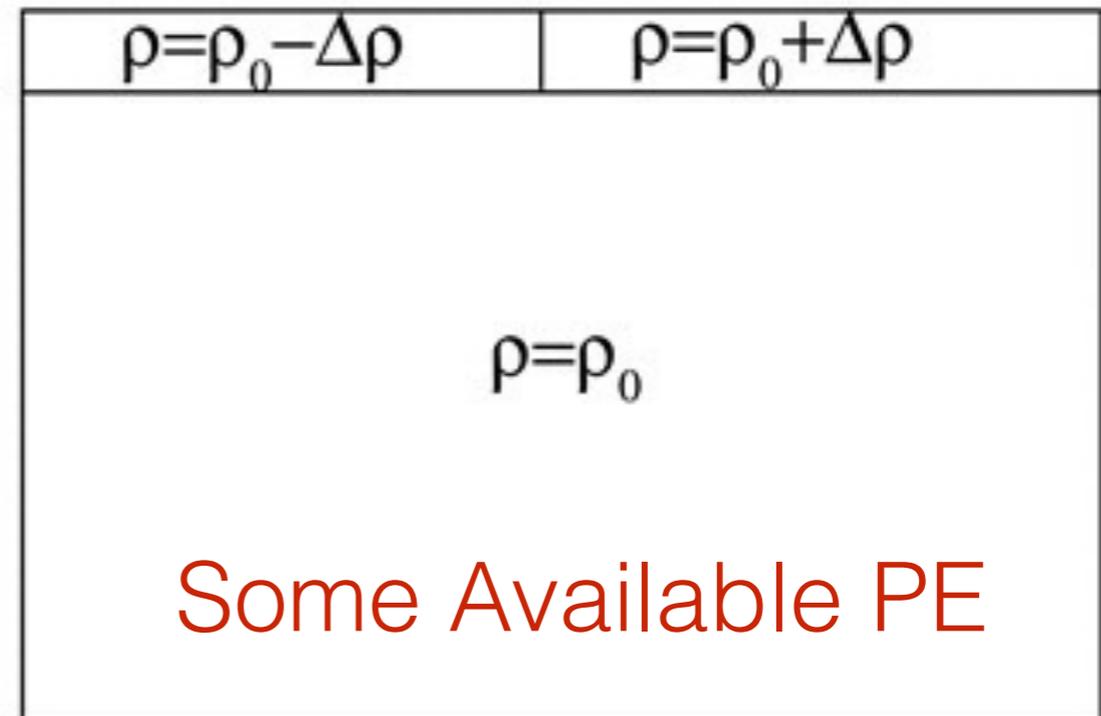
Tailleux (2009); Tailleux and Rouleau (2010)

The same value of potential energy (PE) may reveal very different situations

(a)



(b)



PE = PE_r + APE

Hughes et al., (JPO, 2009)

Lorenz (1955) theory of available potential energy

Boussinesq Momentum Equations

Coriolis

**Buoyancy
+ Wind**

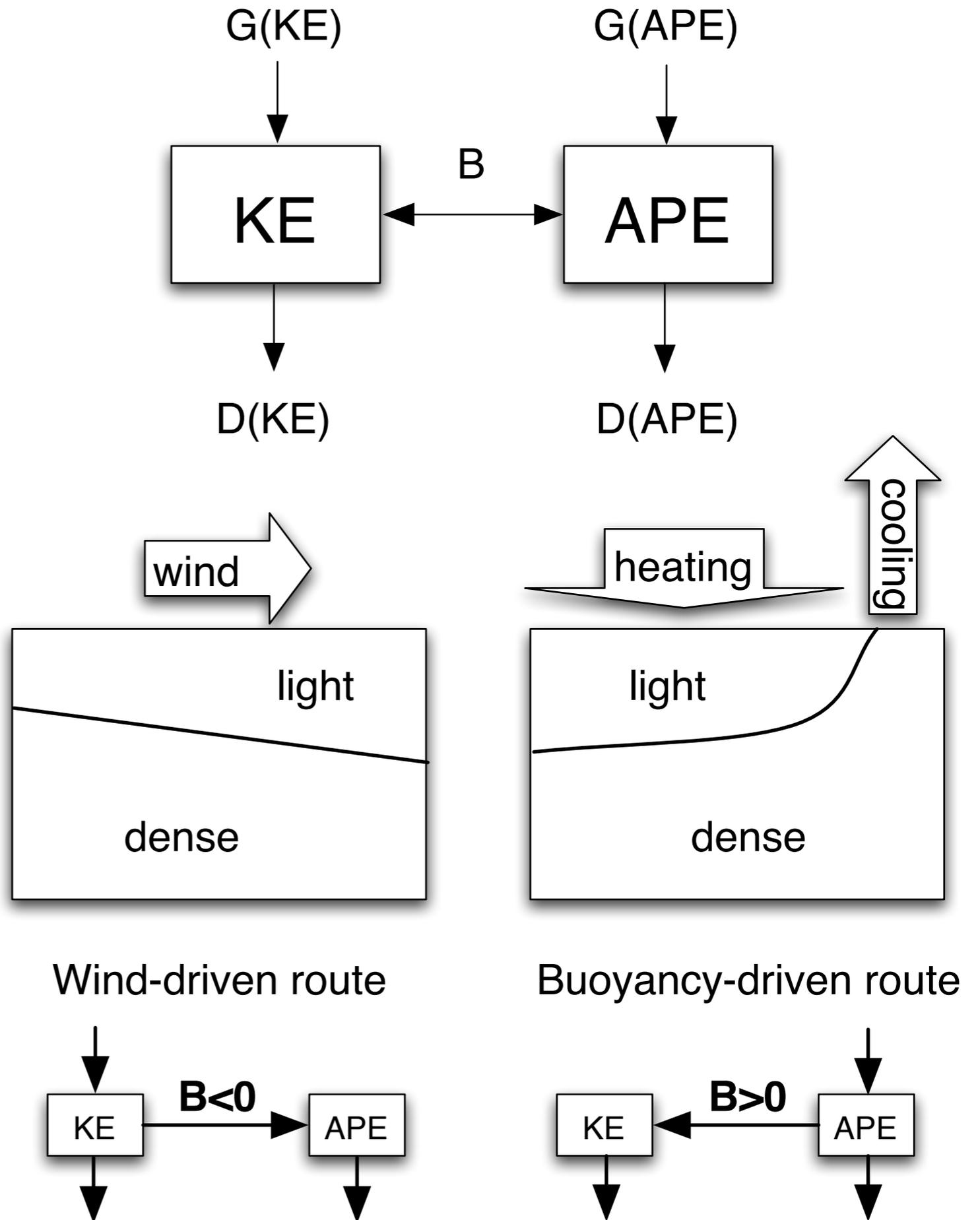
Wind

$$\frac{D\mathbf{u}}{Dt} + f\mathbf{z} \times \mathbf{u} + \frac{1}{\rho_0} \nabla_h(p - p_r(z)) = \frac{\partial}{\partial z} \left(A_v \frac{\partial \mathbf{u}}{\partial z} \right)$$

$$\frac{\partial(p - p_r)}{\partial z} = -g(\rho(S, \theta, z) - \rho_r(z))$$

Wind-driven route versus buoyancy-driven route

*Gregory and Tailleux (2011)
Clim. Dyn.*



Energetics: Filter out Coriolis

Multiply by horizontal velocity

$$\rho_0 \frac{D}{Dt} \frac{\mathbf{u}^2}{2} = -\mathbf{u} \cdot \nabla_h p + \rho_0 \frac{\partial}{\partial z} \left(A_v \frac{\partial \mathbf{u}^2}{\partial z} \right) - \rho_0 A_v \left(\frac{\partial \mathbf{u}}{\partial z} \right)^2$$

Integrate vertically

$$\int_{-H}^0 \rho_0 \frac{D e_k}{Dt} dz = - \int_{-H}^0 \mathbf{u} \cdot \nabla_h (p - p_r) dz + \mathbf{u} \cdot \boldsymbol{\tau}_s - \int_{-H}^0 \rho_0 A_v \left(\frac{\partial \mathbf{u}}{\partial z} \right)^2 dz$$

**APE to KE
conversion**

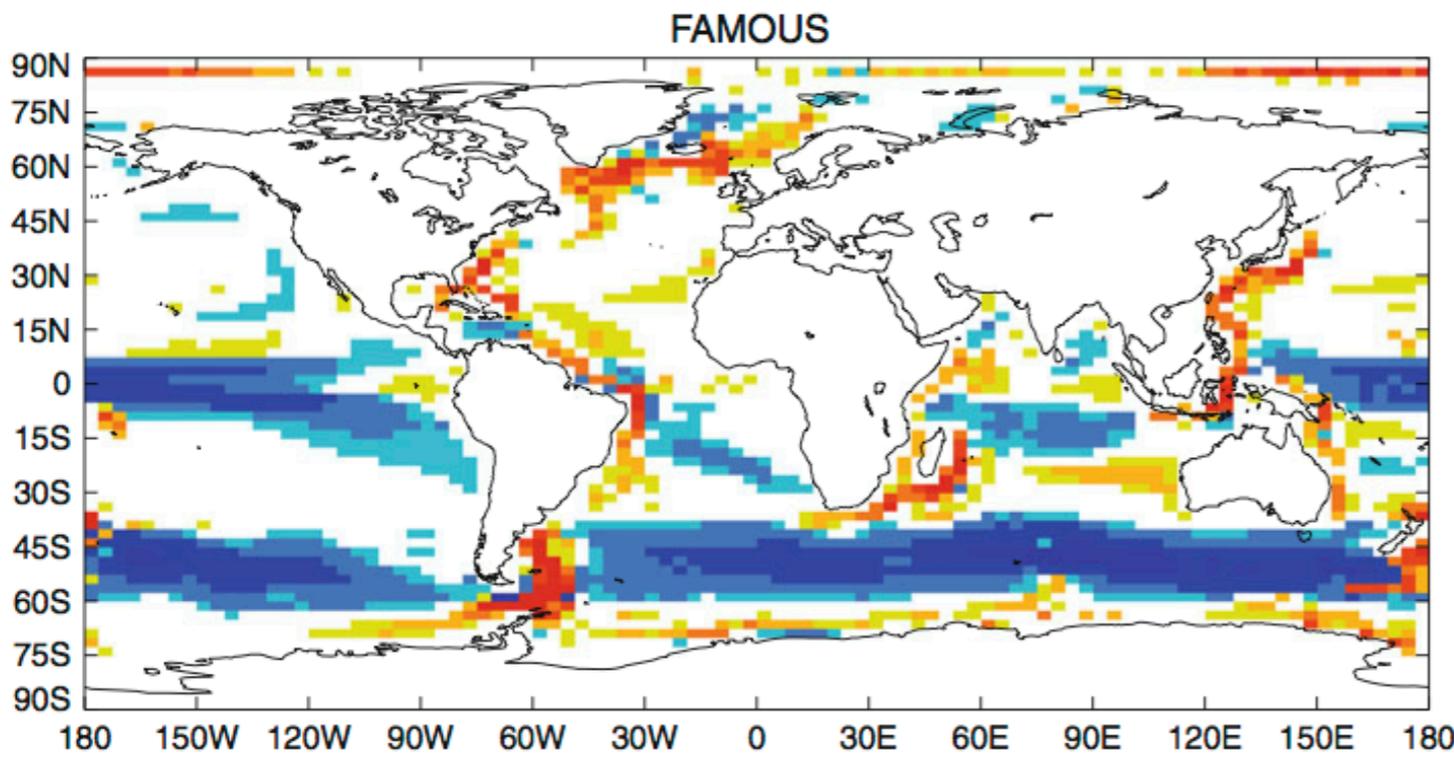
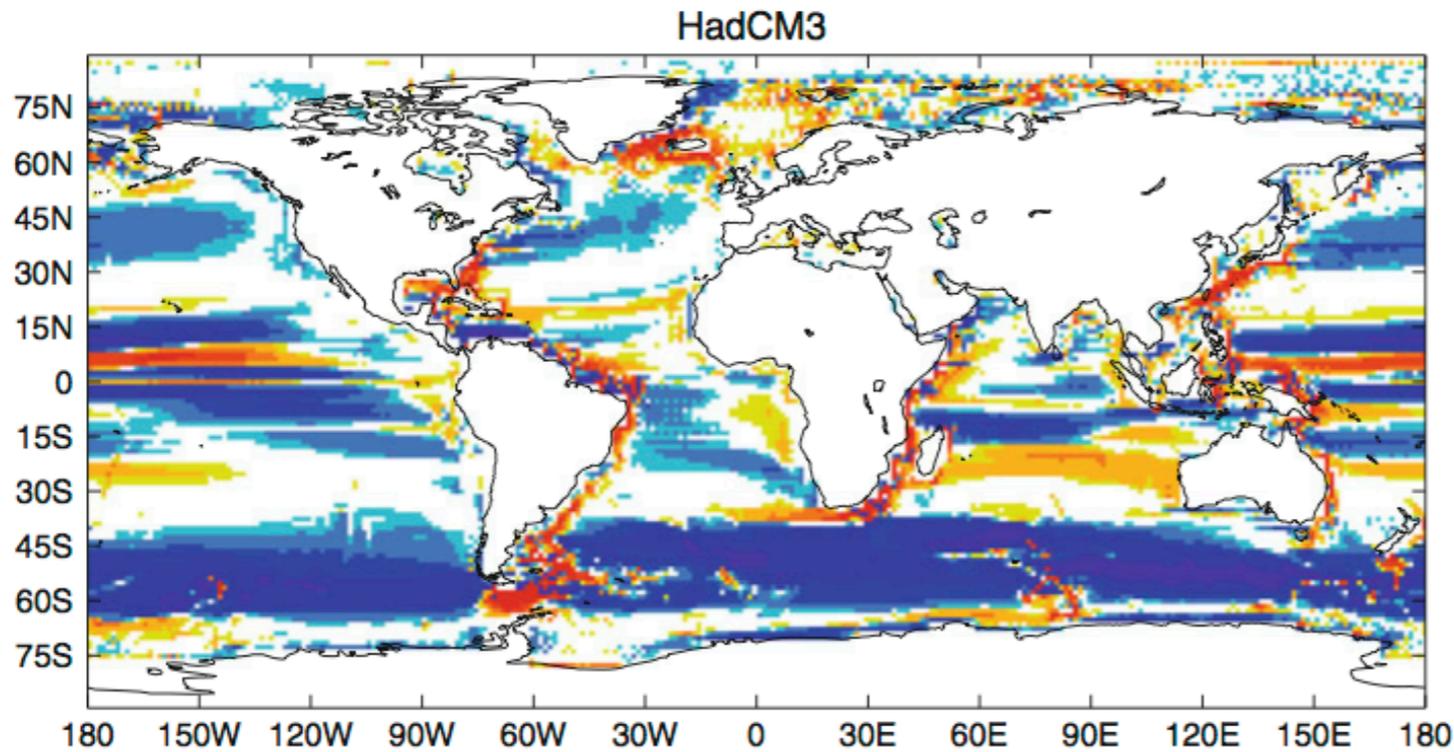
Wind work

**Viscous
Dissipation**

From Gregory and Tailleux, 2011

Local APE to KE Conversion ($\text{mW}\cdot\text{m}^{-2}$)

$$-\int_{-H}^0 \mathbf{u} \cdot \nabla_h P dz$$



**Buoyancy-Driven
Regions
(High Latitudes,
Western Boundaries)**

**Wind-Driven
Regions
(ACC, Equator,...)**

Isolation of the wind forcing and viscous dissipation

$$\int_{-H}^0 \rho_0 \mathbf{u} \cdot \frac{\partial}{\partial z} \left(A_v \frac{\partial \mathbf{u}}{\partial z} \right) dz = \mathbf{u}_s \cdot \boldsymbol{\tau}_s - \int_{-H}^0 \rho_0 A_v \left(\frac{\partial \mathbf{u}}{\partial z} \right)^2 dz$$


Isolation of the buoyancy forcing and mixing?

$$-\int_{-H}^0 \mathbf{u} \cdot \nabla_h (p - p_r) dz = \text{Buoyancy} + \text{Mixing} + \dots$$

Buoyancy-driven theory seeks to link pressure gradient work to surface buoyancy fluxes and interior mixing processes

Local Definition of Available Potential Energy = Work of buoyancy force from rest state to actual state = quadratic positive definite for small amplitude

$$e_a(S, \theta, z) = \int_{z_r(S, \theta)}^z \frac{g(\rho(S, \theta, z') - \rho_r(z'))}{\rho_0} dz' \approx \frac{N^2 (z - z_r)^2}{2}$$

APE density satisfies local evolution equation

$$\rho_0 \frac{De_a}{Dt} = (\rho - \rho_r)gw - \rho_0 \alpha g(z - z_r) \frac{D\theta}{Dt} + \rho_0 \beta g(z - z_r) \frac{DS}{Dt}$$

Manipulate and integrate vertically

$$-\int_{-H}^0 \mathbf{u} \cdot \nabla (p - p_r) dz = \rho_0 g |z_r| \left(\beta S_0 (E - P) - \frac{\alpha Q}{c_p} \right) - \int_{-H}^0 \rho_0 K_v N_r^2 dz - \int_{-H}^0 \rho_0 \frac{De_a}{Dt} dz - \nabla \cdot \int_{-H}^0 p' \mathbf{u} dz$$

Production by surface buoyancy fluxes

Dissipation by Mixing

Horizontal Transfers

State Dependent Wind and Buoyancy Forcing

Wind Forcing depends on Ocean Surface Velocity

$$G(KE) = \iint_S \mathbf{u}_s \cdot \boldsymbol{\tau}_s dx dy$$

Buoyancy Forcing depends on Lorenz Reference Depth

$$G(APE) = \iint_S g |z_r| \left(\rho_0 \beta S_0 (E - P) - \frac{\alpha Q}{c_p} \right) dx dy$$

Buoyancy-Driven Theory of the AMOC

Unknown Proportionality Factor

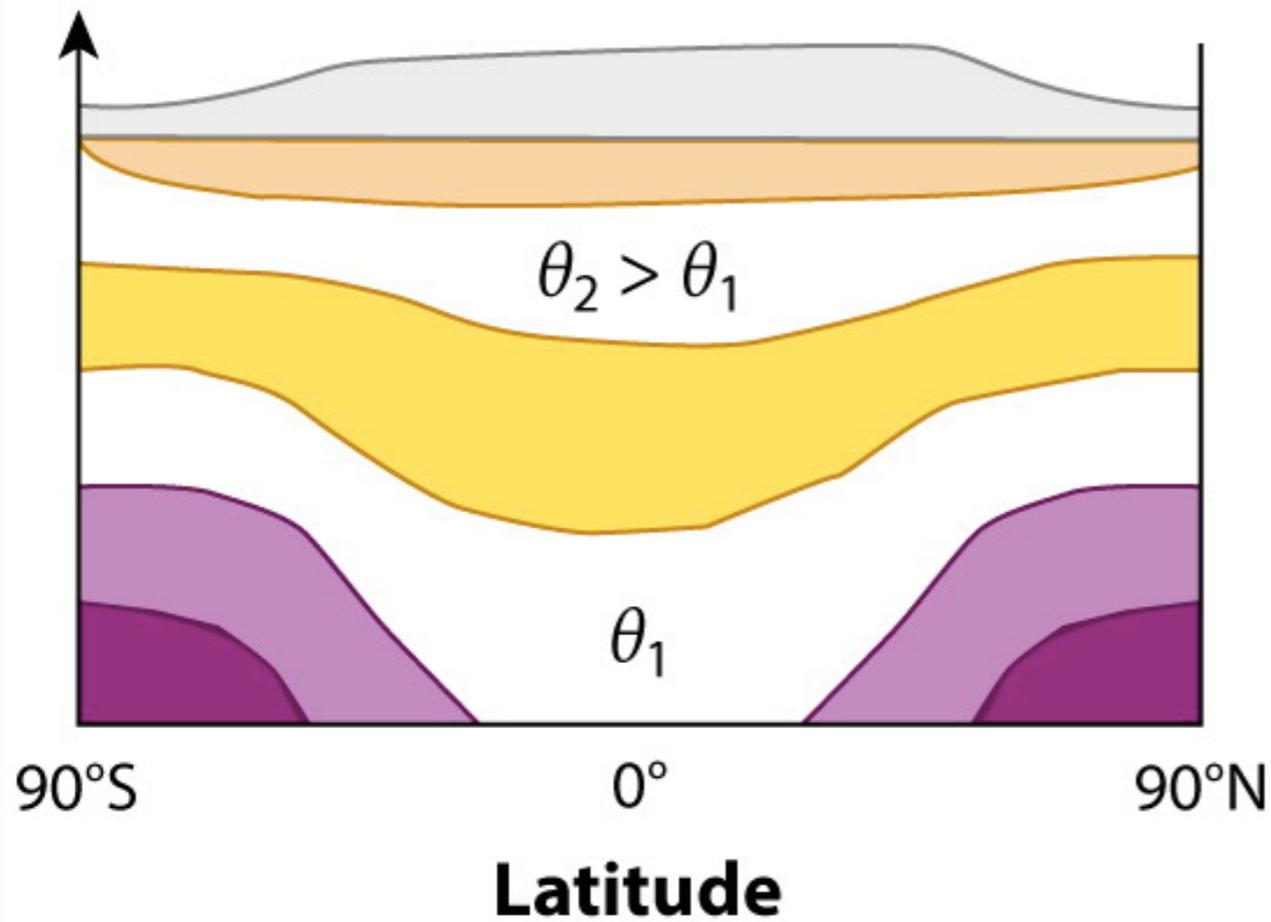
$$\Psi_{AMOC} = k_{atlantic} \iint_{Atlantic} g |z_r| \left(\rho_0 \beta (E - P) - \frac{\alpha Q}{c_p} \right) dx dy$$

Mechanically-controlled
Reference Depth
(e.g., mixing)

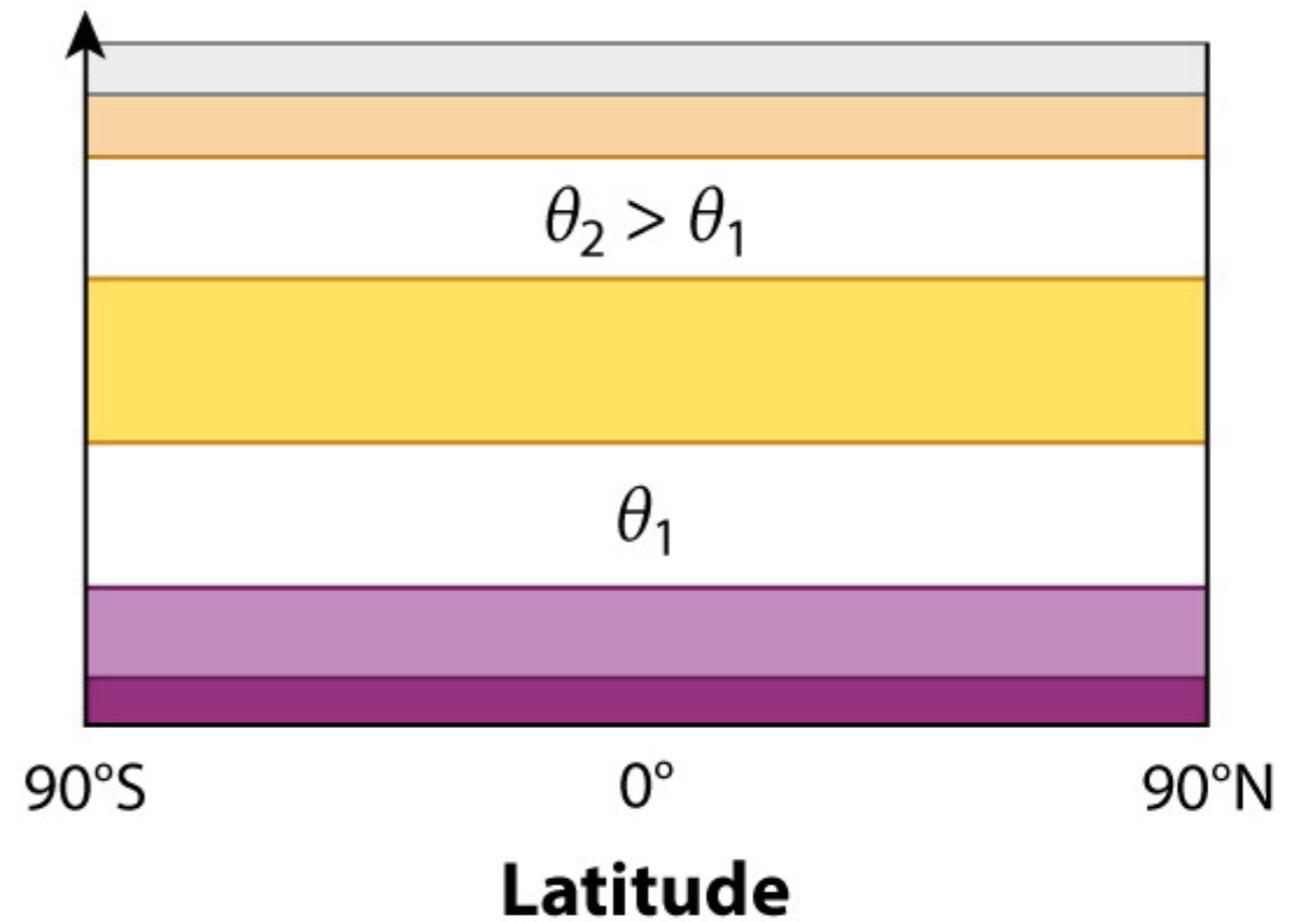
Buoyancy Forcing

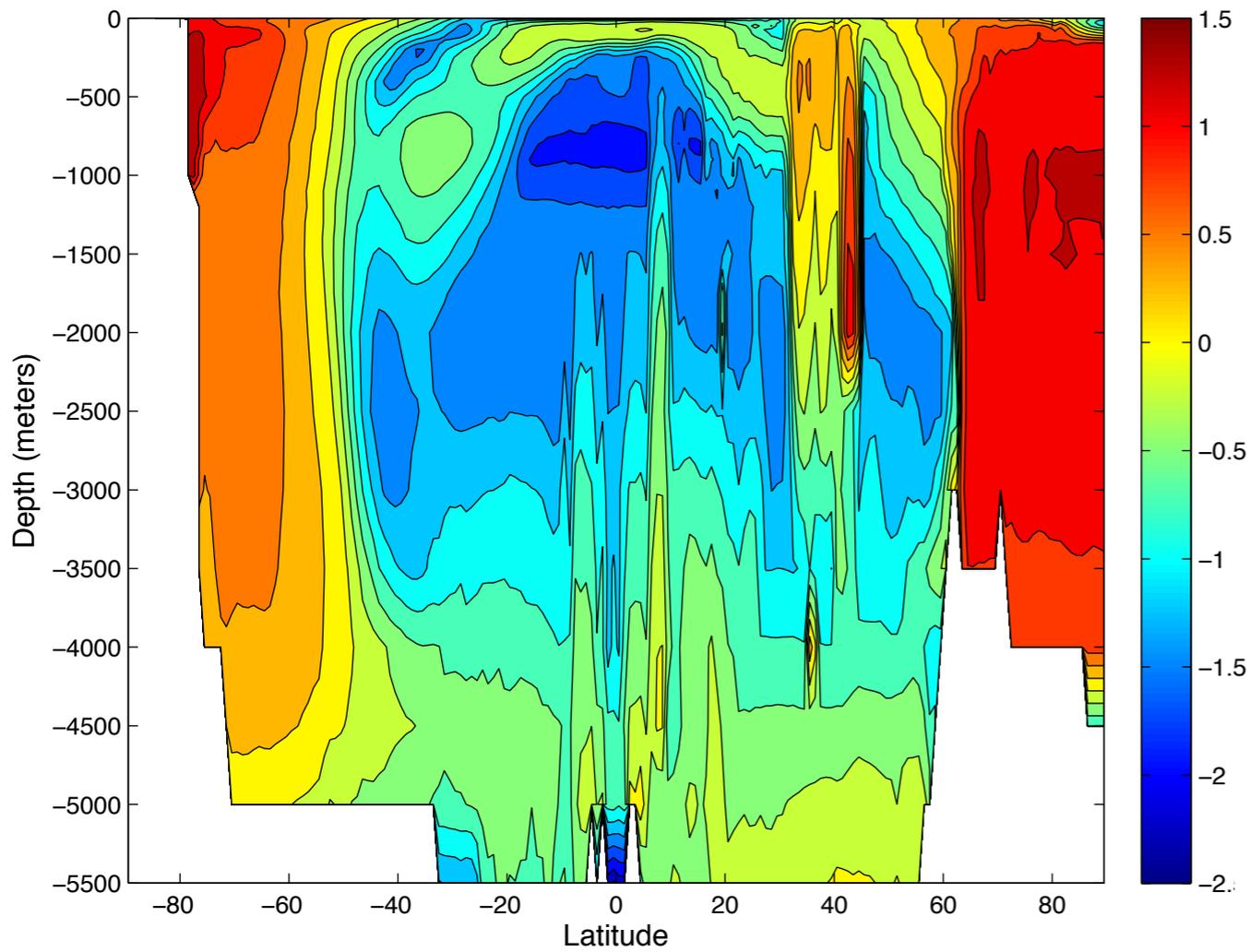
Lorenz (1955) theory of available potential energy and its moist extension (1978, 1979)

a Actual state

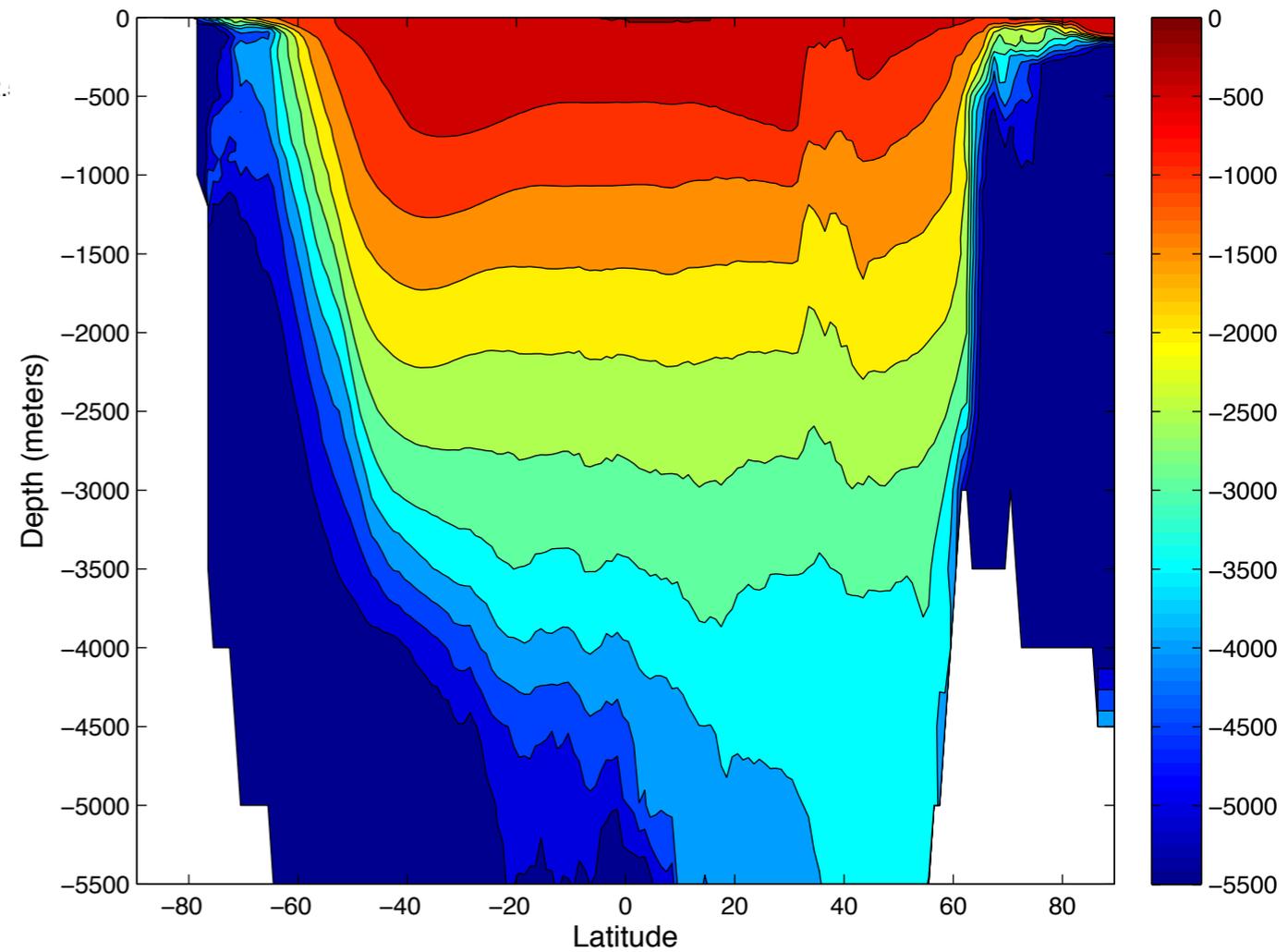


b Reference state



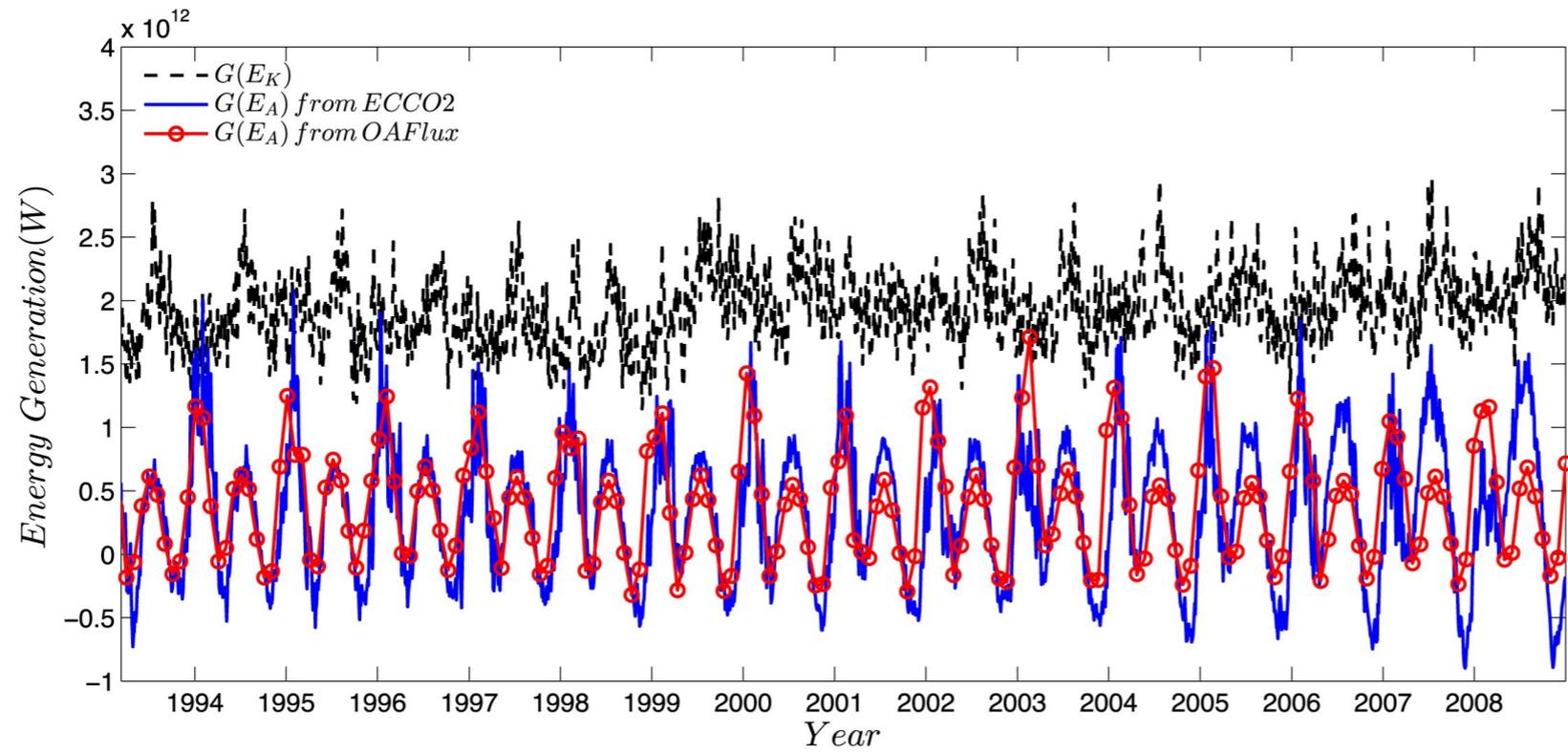


Decimal Logarithm of zonally-averaged APE density

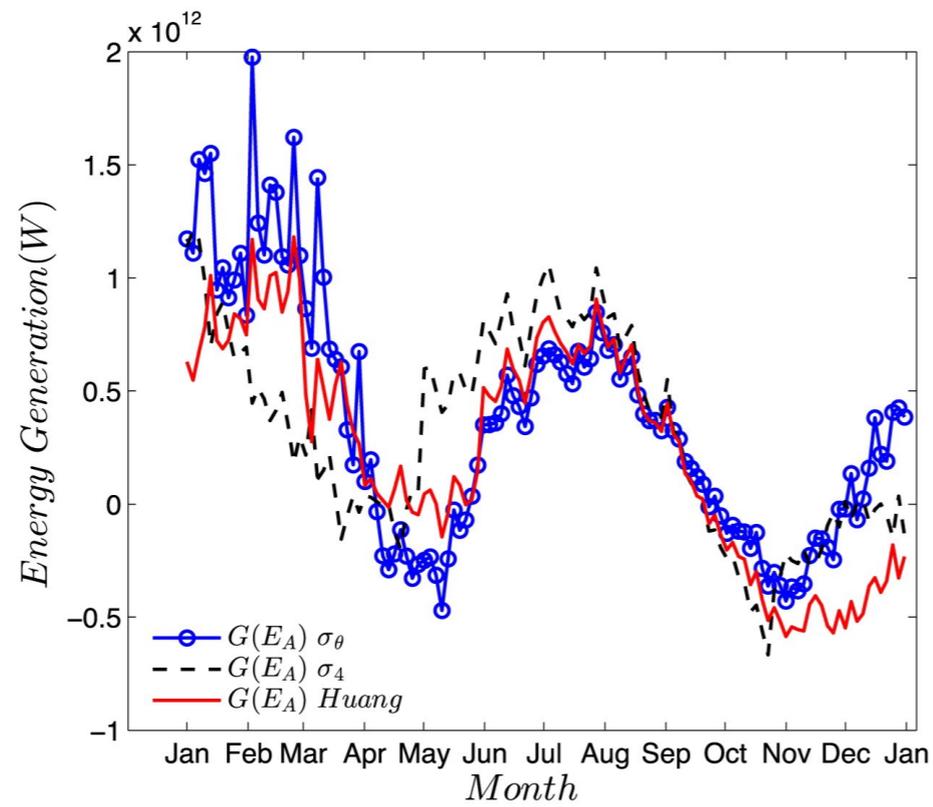


Zonally-averaged
Reference position

Tailleux 2013, Saenz et al. (2015)



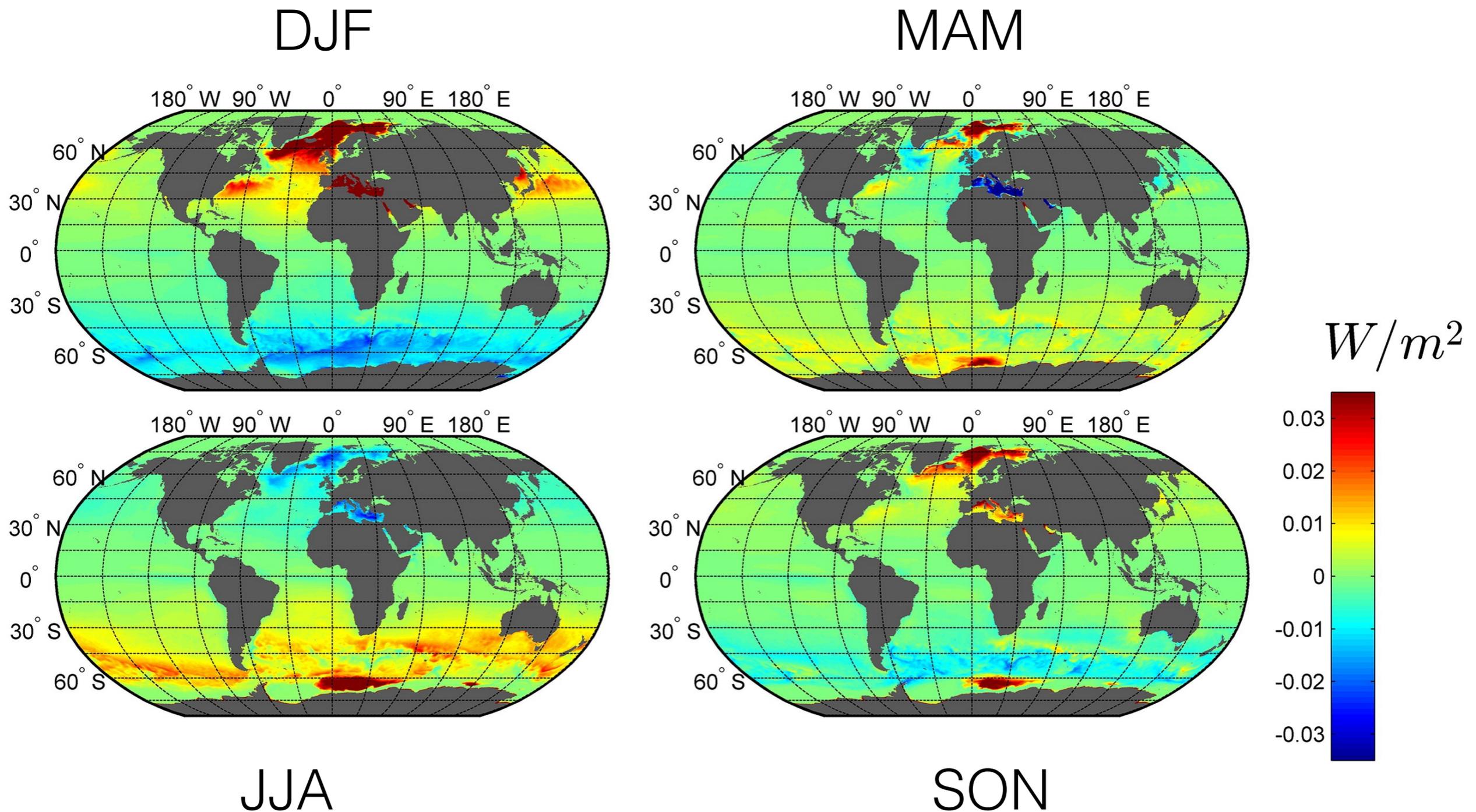
(a)



(b)

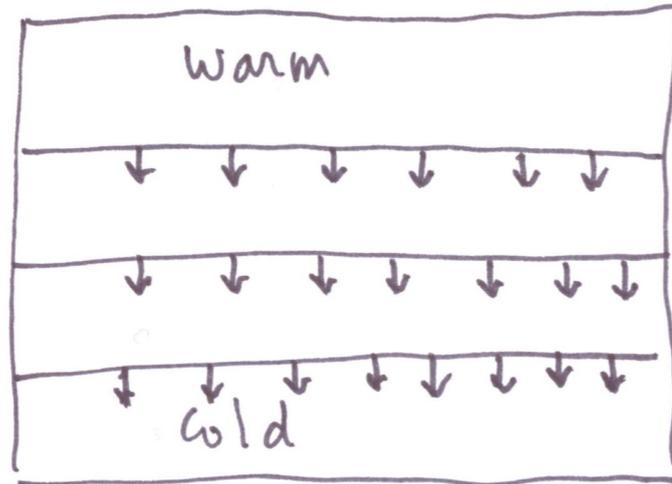
Seasonally averaged APE generation rate from ECCO2

From Zemkova et al. (JPO, 2015)



Increasing mixing controls
 $G(\text{APE})$ through increasing
thermocline depth

Laminar case

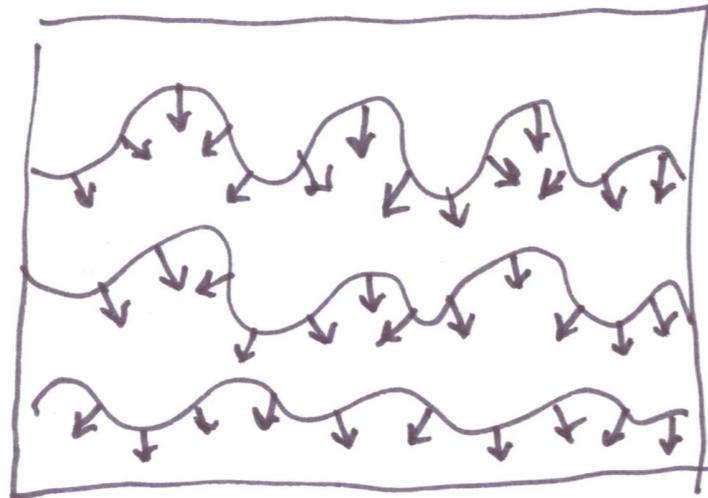


Total Heat Flux =

$$-k_T A_{\text{laminar}} \rho C_p \frac{\partial T}{\partial z}$$

$$= F_{\text{laminar}}$$

Turbulent case



Total heat flux =

$$-k_T A_{\text{turbulent}} \rho C_p \left\langle \frac{\partial T}{\partial n} \right\rangle$$

$$= F_{\text{turbulent}}$$

One shows that: $\left\langle \frac{\partial T}{\partial n} \right\rangle \approx \frac{A_{\text{turbulent}}}{A_{\text{laminar}}} \times \frac{\partial T}{\partial z}$

$$\Rightarrow F_{\text{turbulent}} = \left(\frac{A_{\text{turbulent}}}{A_{\text{laminar}}} \right)^2 F_{\text{laminar}}$$

Bryan (JPO, 1987): Thermocline depth and AMOC strength increase with vertical diffusivity

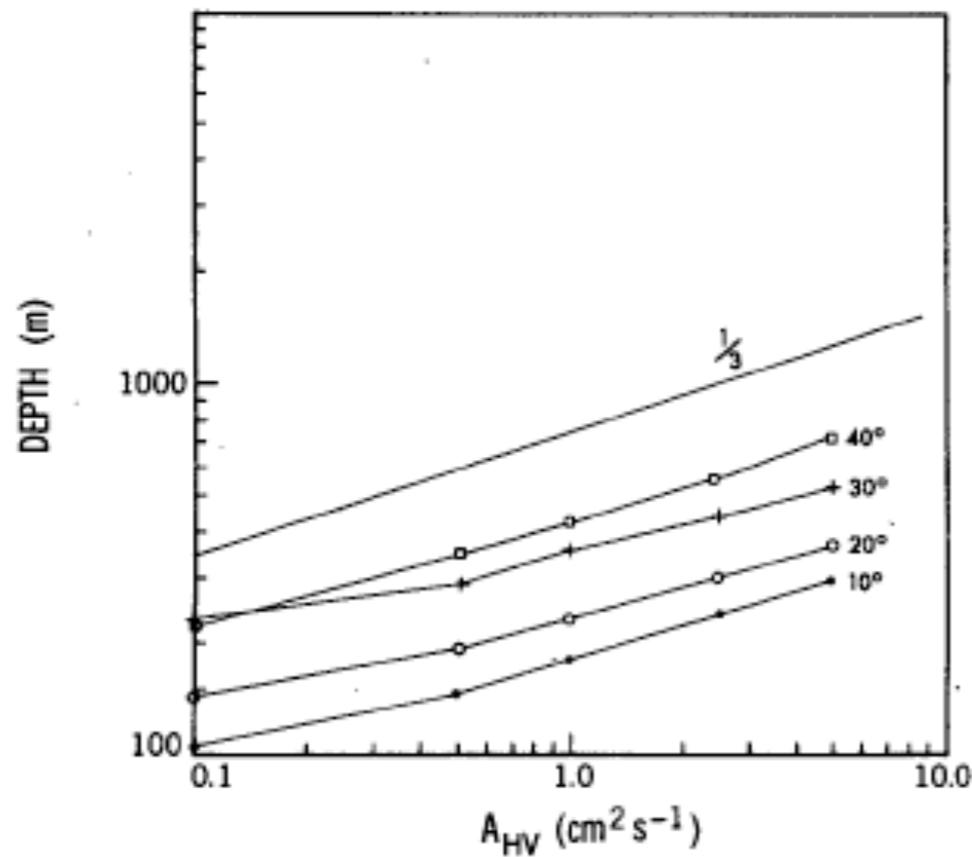


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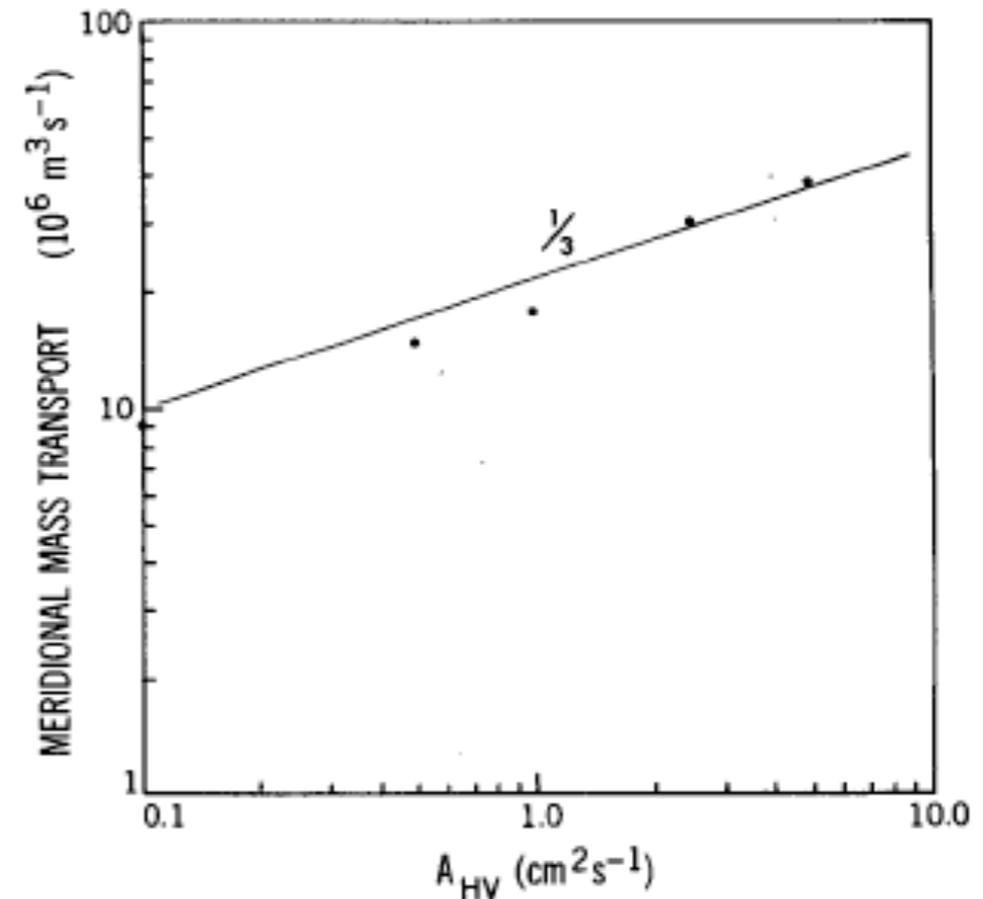
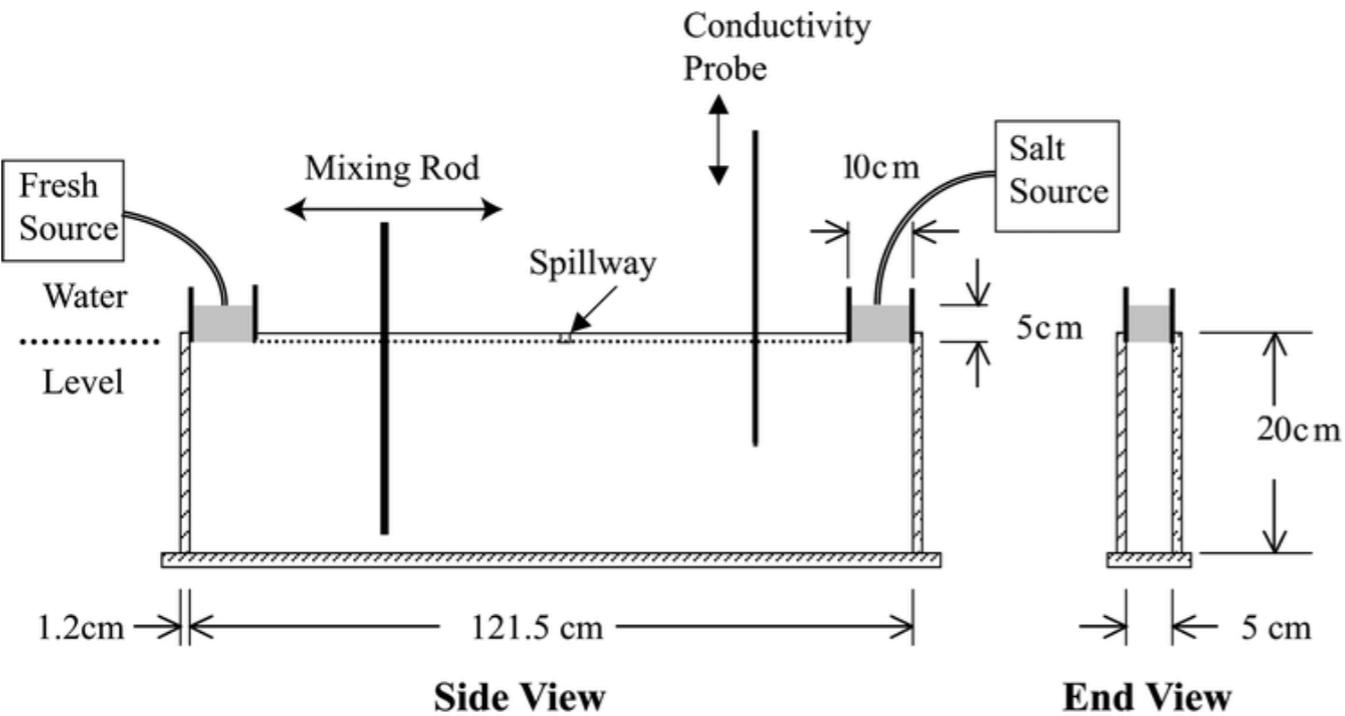


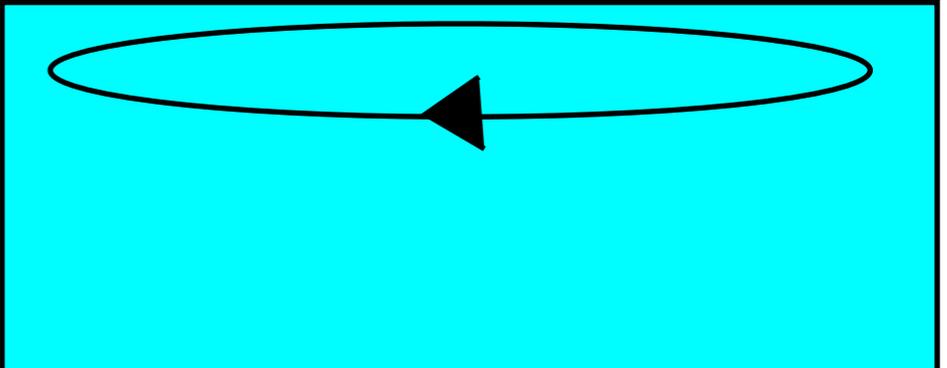
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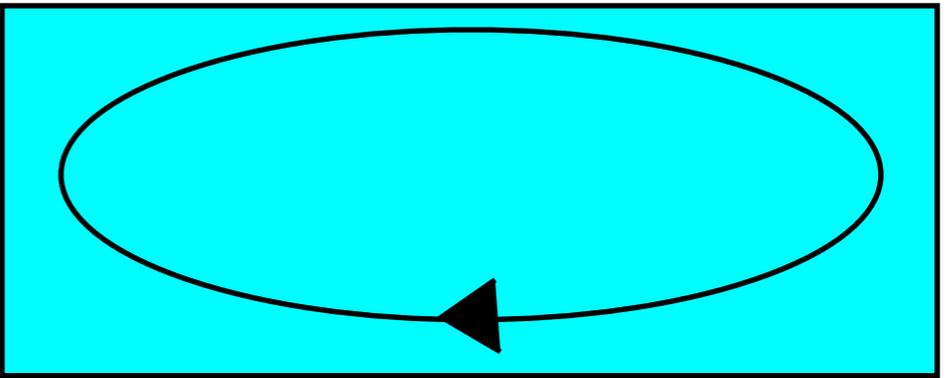
Whitehead and Wang (JPO,2008)



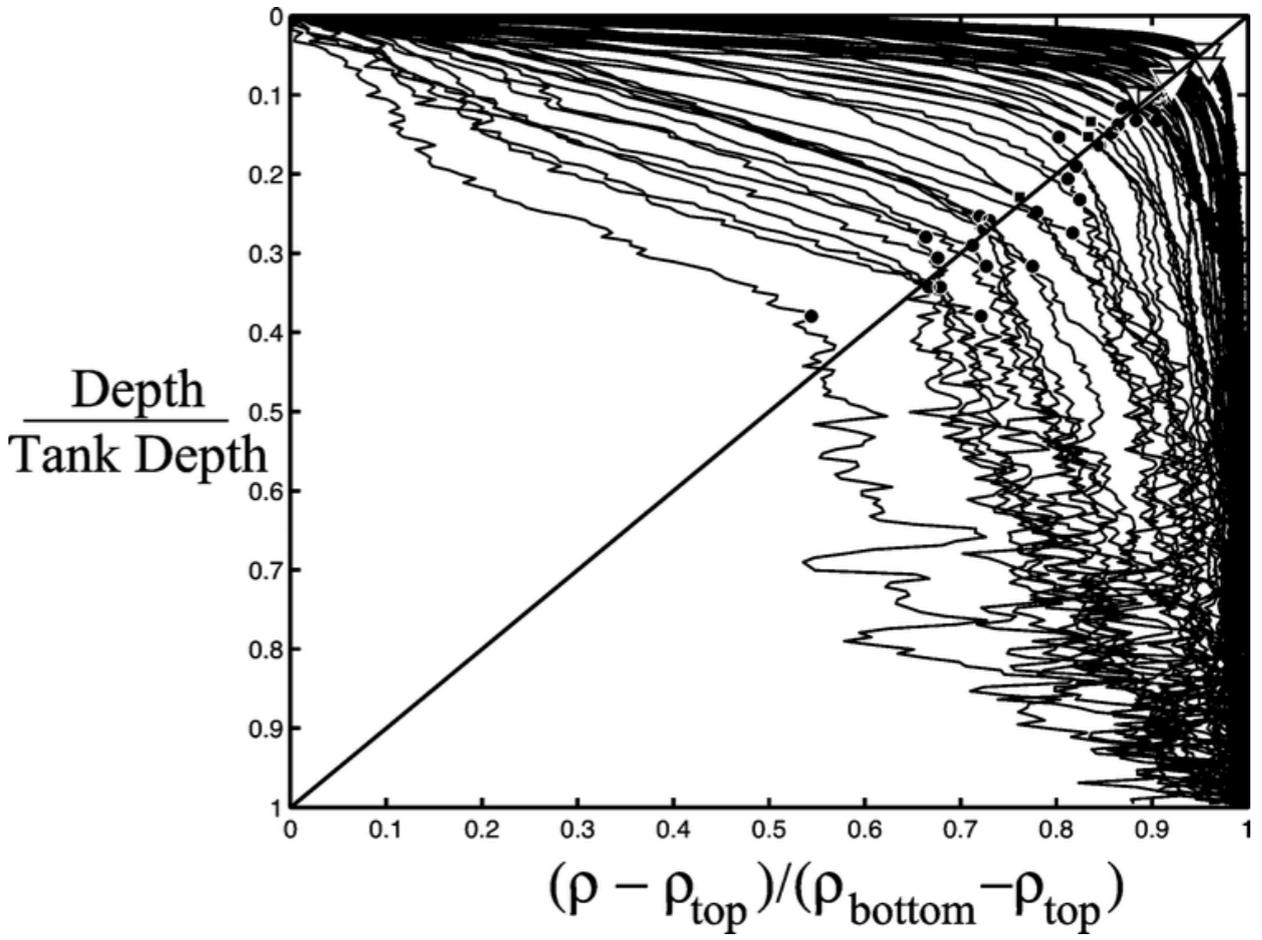
Buoyancy only



Buoyancy + Stirring



Stirring causes stratification to deepen, increasing APE production, increasing overturning



Increase in zonal wind at Drake Passage
increases net heating over ACC, which in
steady state requires increasing net
cooling in Northern Polar Regions thus
increasing $G(APE)$ and AMOC

Atlantic deep circulation controlled by heating in the Southern Ocean

Hiroyasu Hasumi and Nobuo Suginozara

Center for Climate System Research, University of Tokyo, Japan

Abstract. Thermohaline circulation has been considered to be driven by localized buoyancy loss through the sea surface at high latitudes and broadly distributed buoyancy gain elsewhere. Our numerical modeling study, however, shows that buoyancy gain for the Atlantic deep circulation is localized in the Southern Ocean. Wind-induced upwelling there causes efficient heat transfer to the deep ocean, and controls intensity of the Atlantic deep circulation as thermohaline circulation.

buoyancy loss of North Atlantic Deep Water (NADW) in the northern North Atlantic and buoyancy gain somewhere else. Here we try to answer this question by carrying out numerical experiments.

Model and Experiments

The OGCM used in this study is CCSR-OGCM [Hasumi and Suginozara, 1999a] with the Uniformly Third-Order Polynomial Interpolation Algorithm (UTOPIA) [Leonard

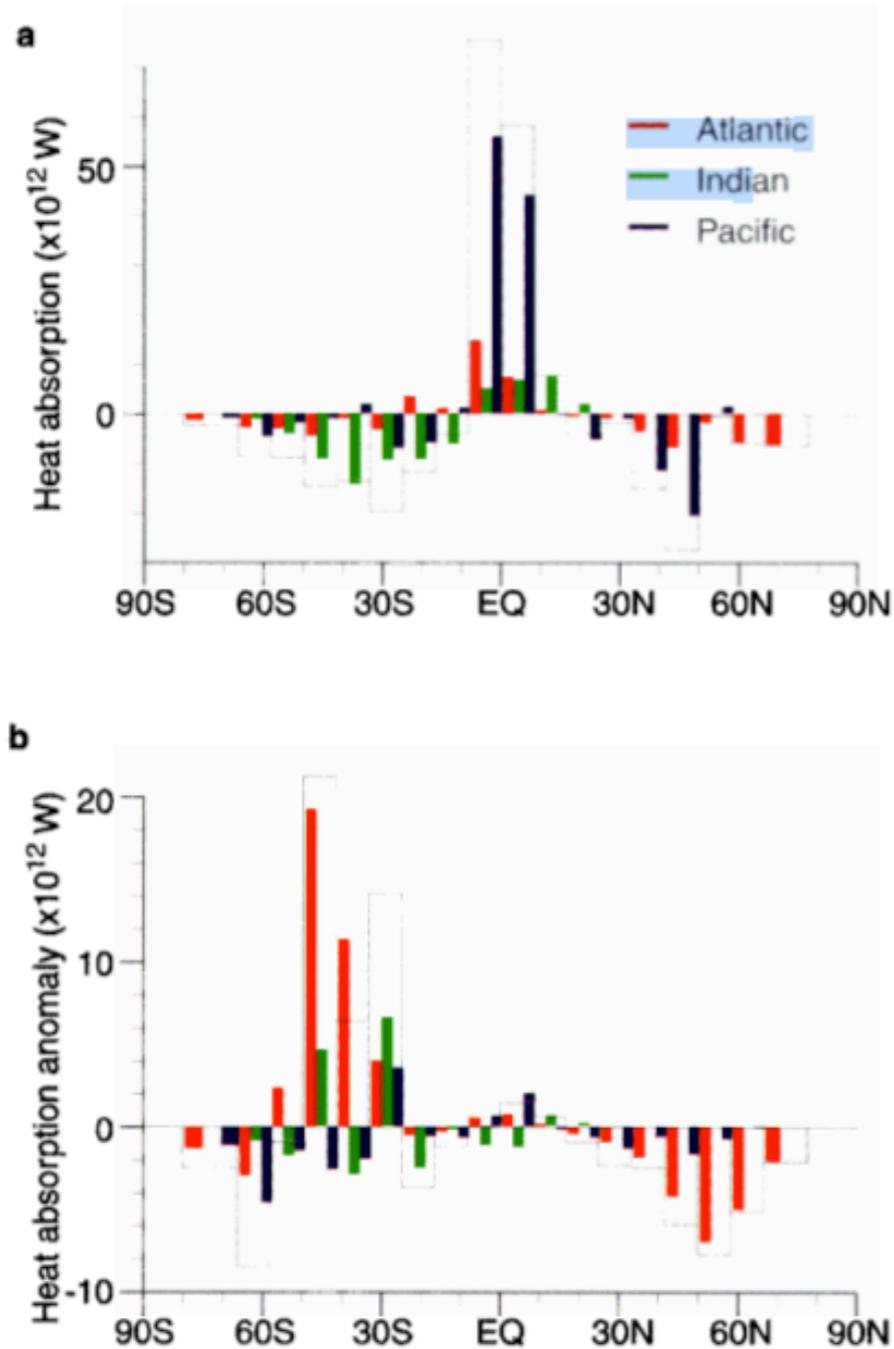
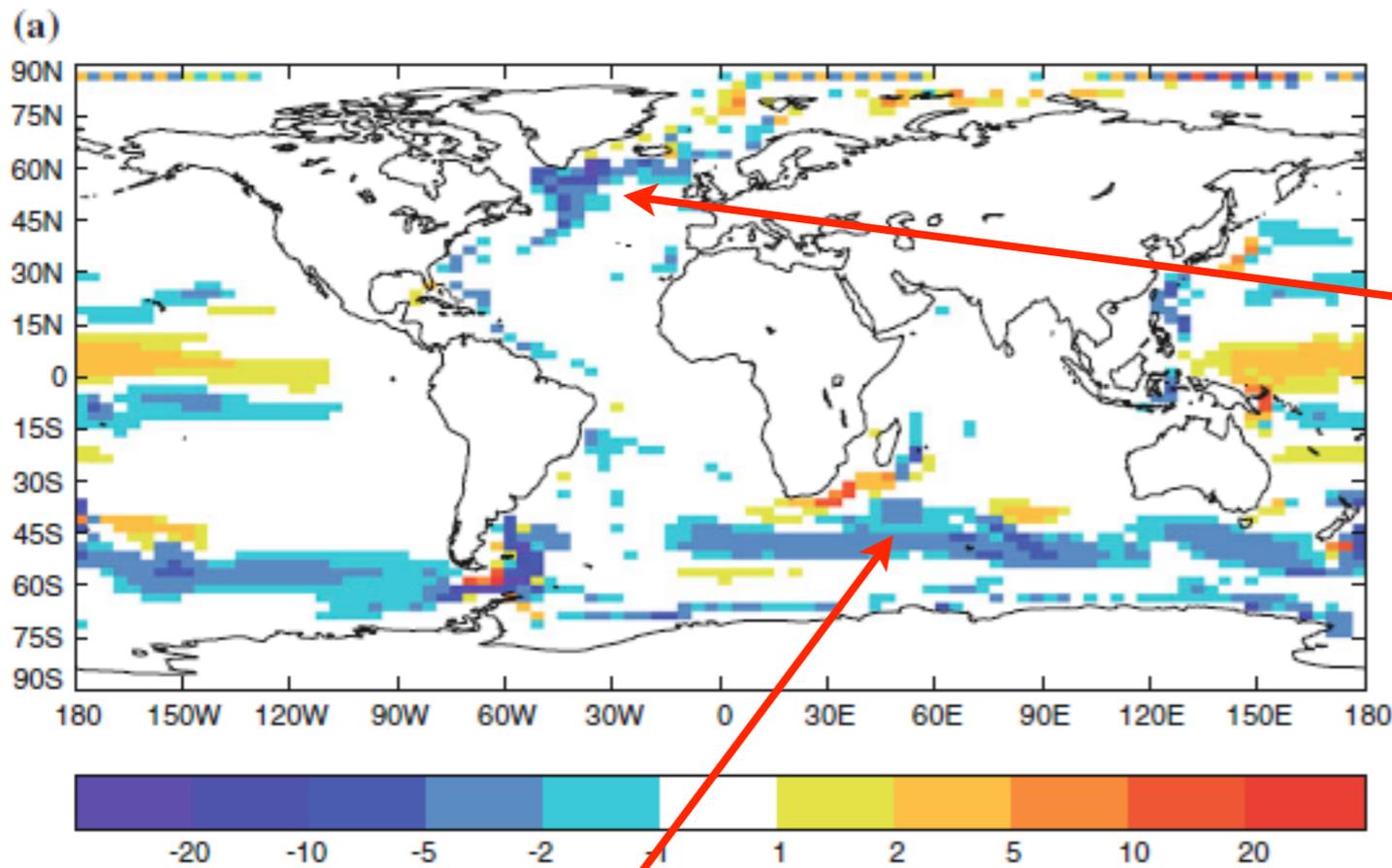


Figure 3. (a) Annual-mean heat flux for the case of no wind stress over the Southern Ocean. Each box shows heat absorbed by the ocean in the latitudinal band indicated by the width of the box. Contribution of each oceanic basin is shown by color bars. (b) Anomaly from (a) for the control case.

Hasumi and Suginozara (1999)

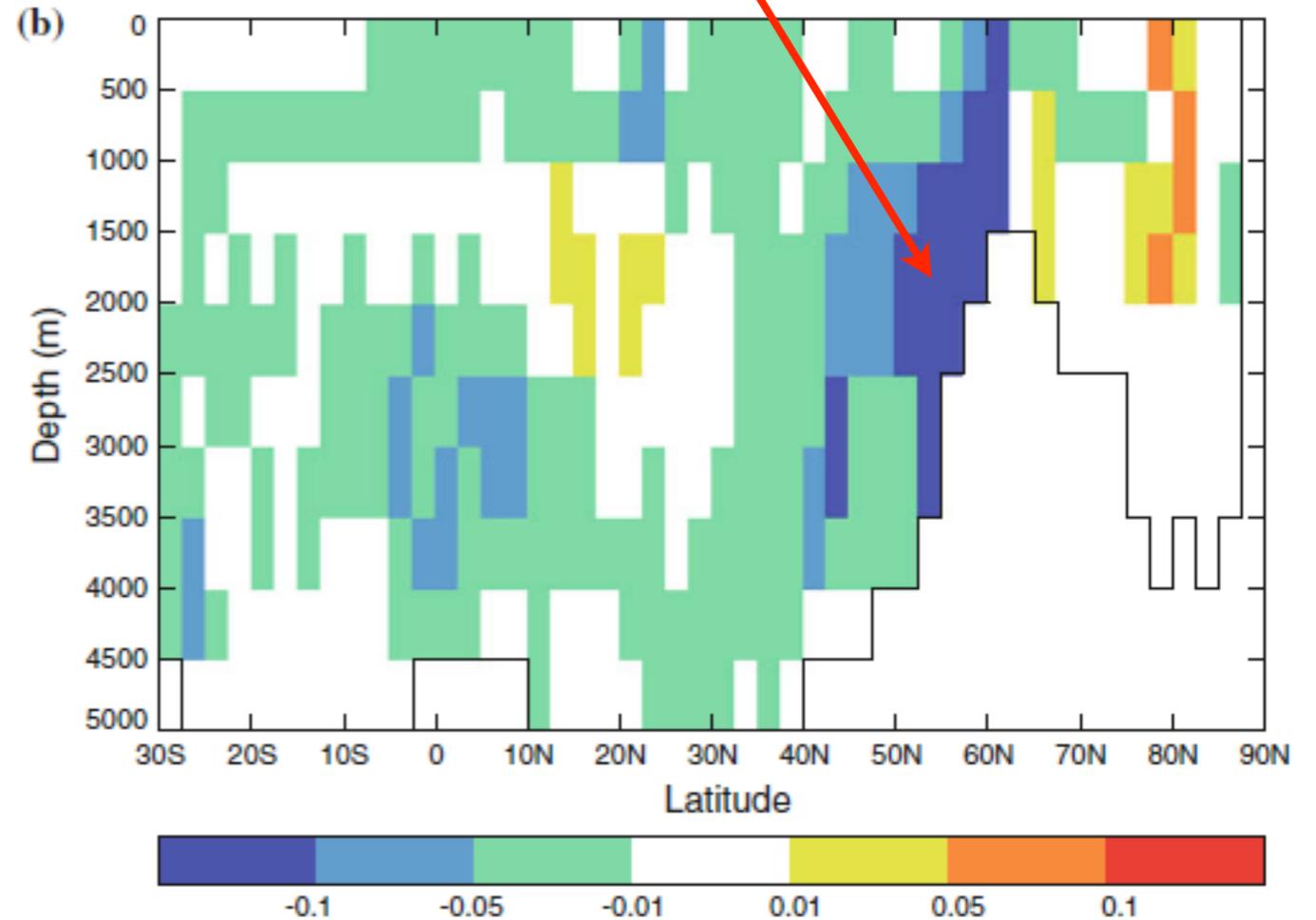
Climate Change



From Gregory and Tailleux, 2011

Global warming
reduces APE production
by buoyancy

Global warming
increases APE
production by the
wind



Conclusions

- Buoyancy-driven theory posits that AMOC strength proportional to APE production rate by high-latitude cooling. Physics of proportionality constant not really understood though: research needed!
- APE production rate is state dependent. Ocean is a mechanically-controlled heat engine. Mixing and winds helps buoyancy forcing out.
- Determination of ocean stratification as important as determination of formation rates for inferring past AMOC variations